

(NOT " $\mu^S SR$ "!)



$\mu^- SR$ IN NUCLEI WITH SPIN

Jess H. Brewer

Canadian Institute for Advanced Research
and Dept. of Physics & Astronomy,
Univ. of British Columbia
Vancouver, BC, Canada

HUH? WUZZAT?

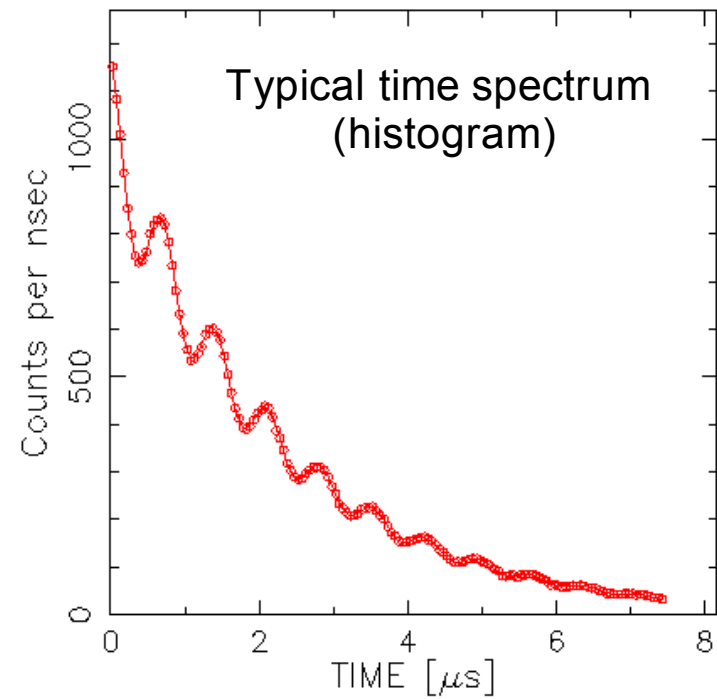
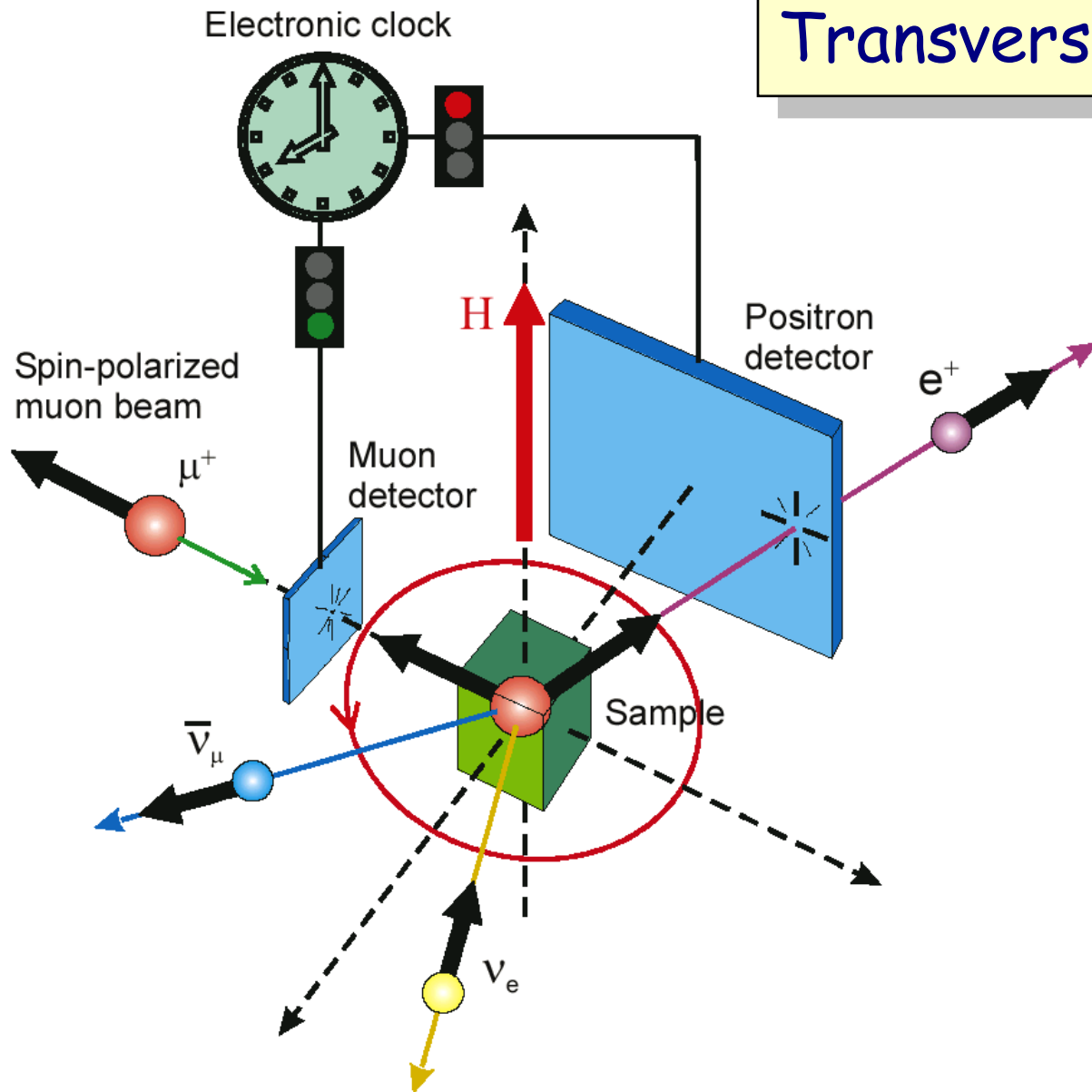
μ SR rotation
relaxation
resonance

m s Applied*
u p Elementary
o i Particle
n n Physics

*(to basic research in
Materials Science
and Chemistry)

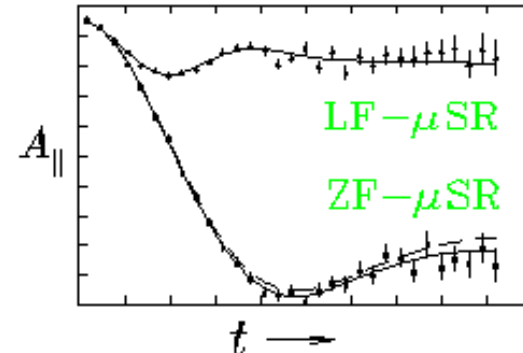
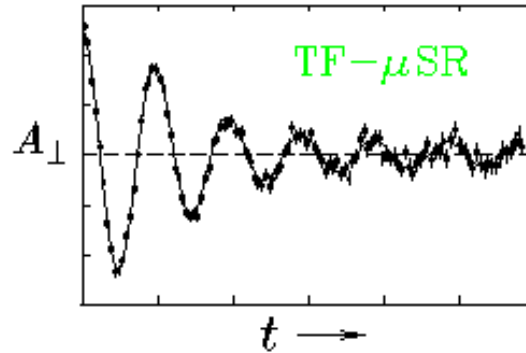
Visit <http://musr.org>

Transverse Field (TF) μ^+SR



Brewer's List of μ SR Acronyms

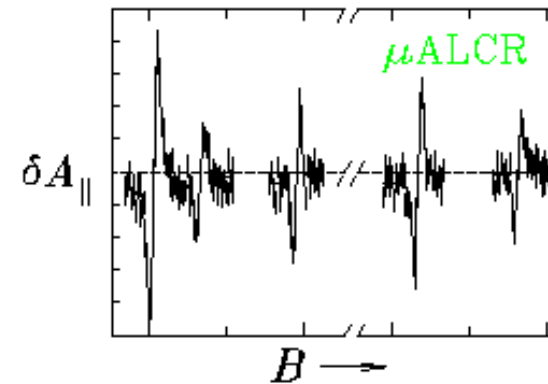
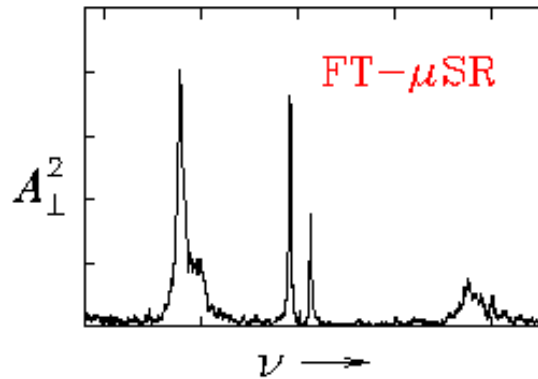
Transverse
Field



Longitudinal
Field

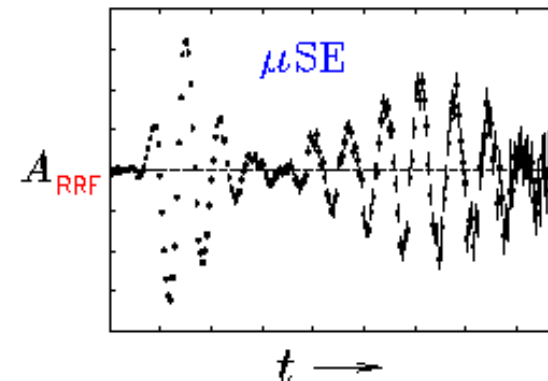
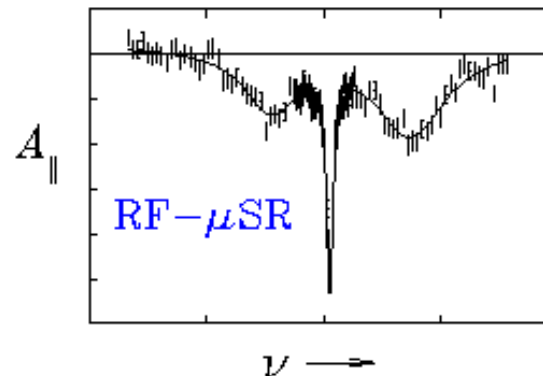
Zero Field

Fourier
Transform
 μ SR



Avoided
Level
Crossing
Resonance

Muon
Spin
Resonance

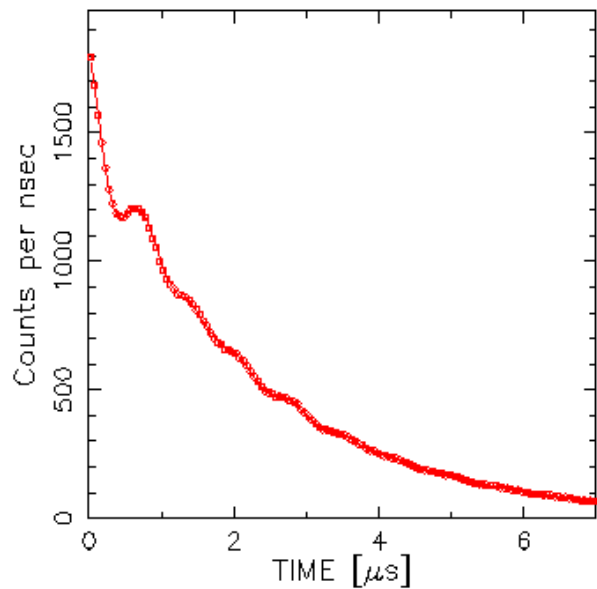


Muon
Spin
Echo

μ^+SR

vs.

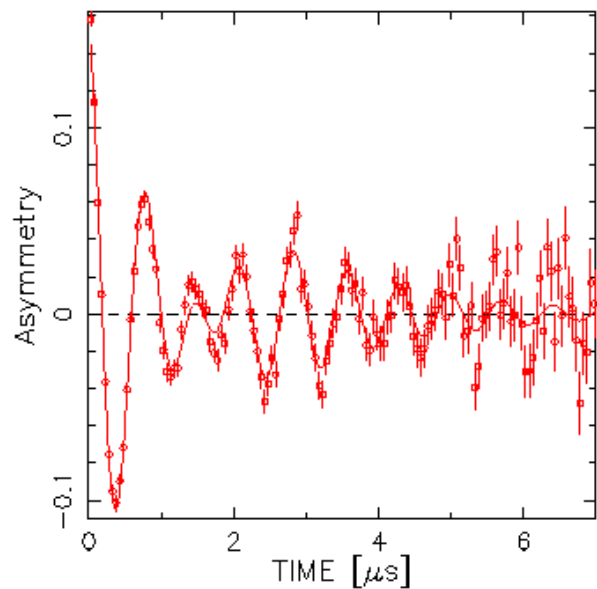
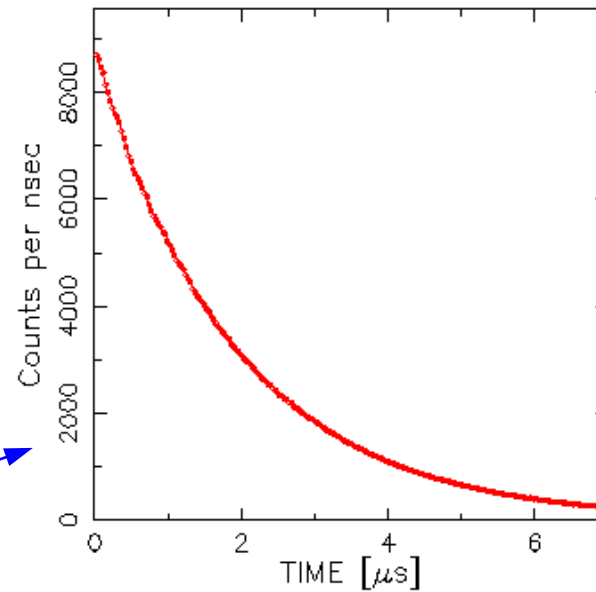
μ^-SR



Typical time spectrum (histogram)

Single lifetime $\tau_\mu = 2.197 \mu s$

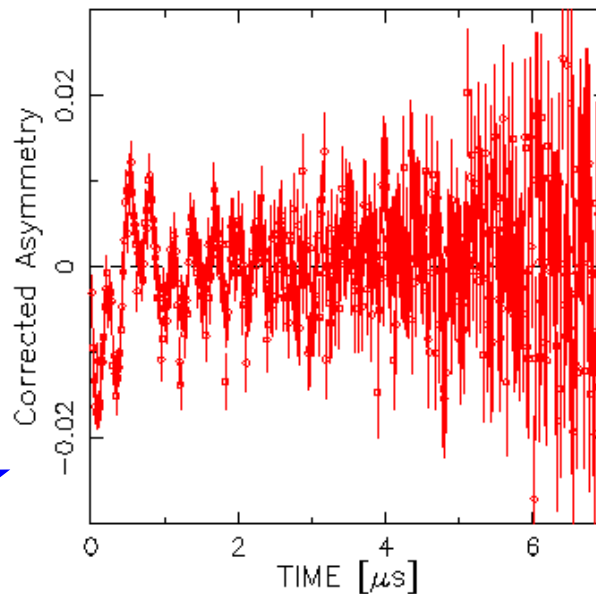
Multiple lifetimes (some very short!)



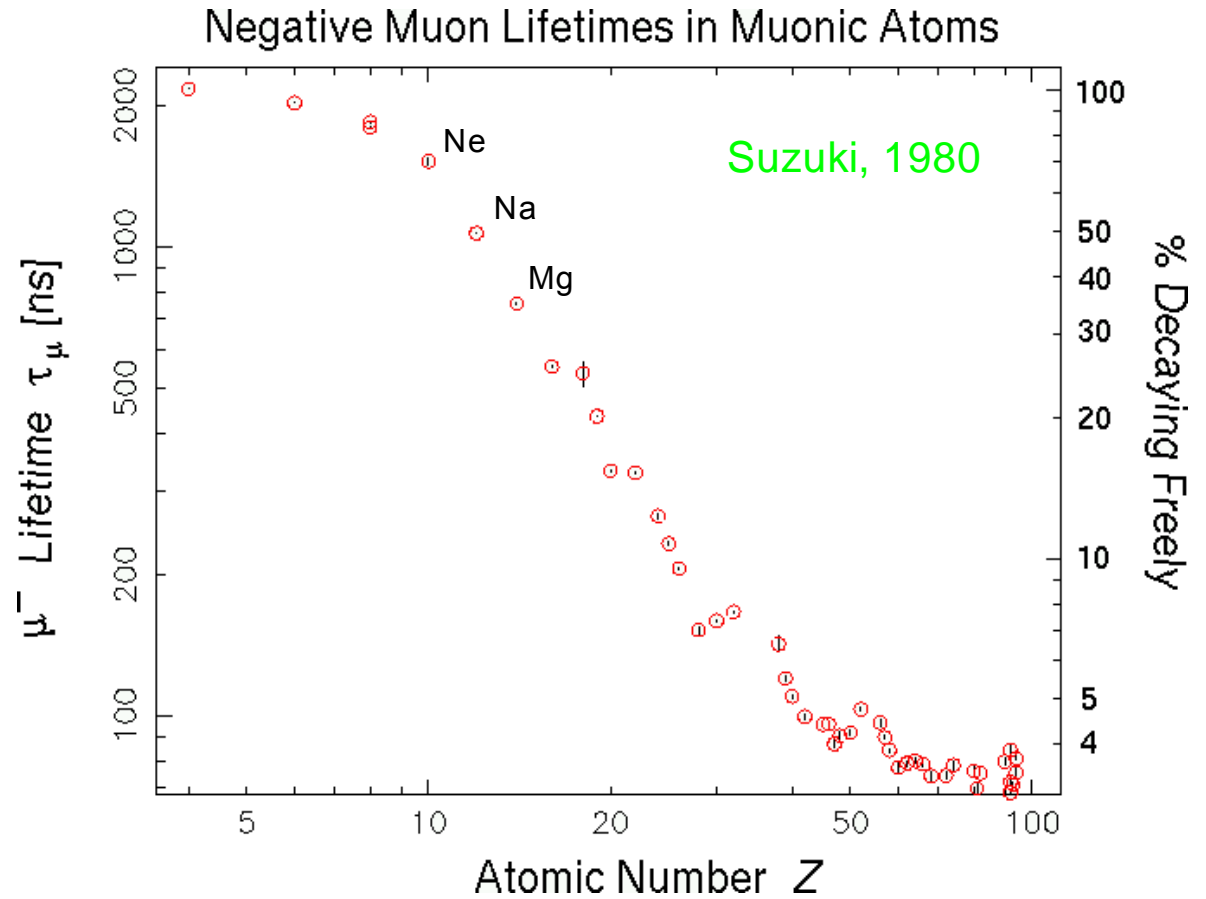
Asymmetry spectrum

Large amplitudes

Small amplitudes



Nuclear
 μ^-
 Capture

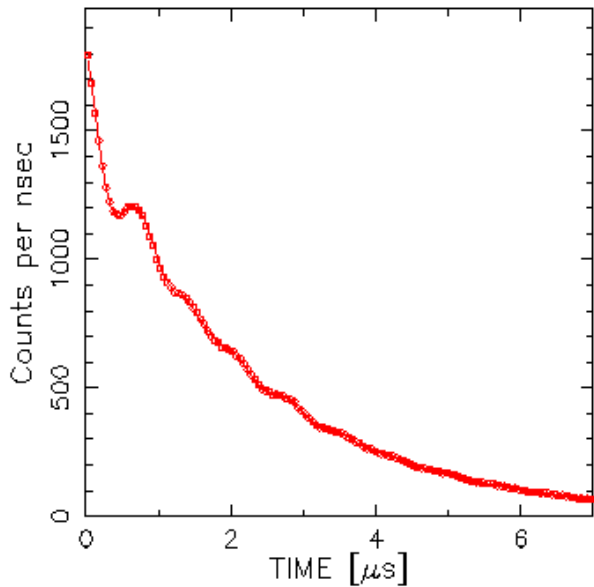


Rate exceeds that of $\mu^- \rightarrow e^- \nu_\mu \nu_e$ for $Z \geq 11$.

μ^+SR

vs.

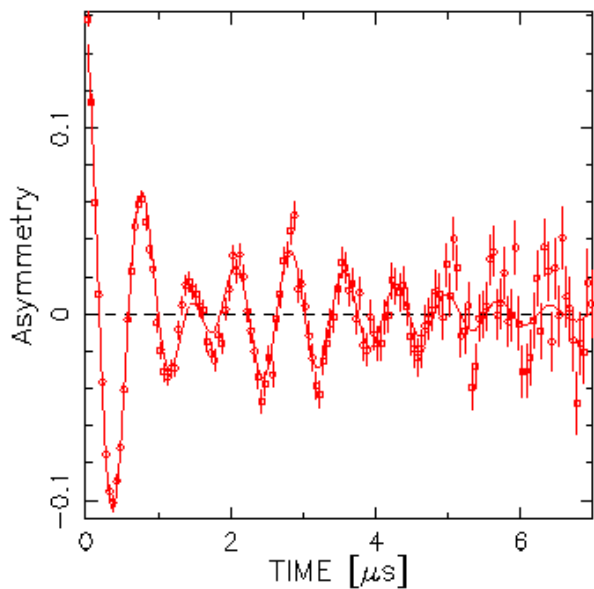
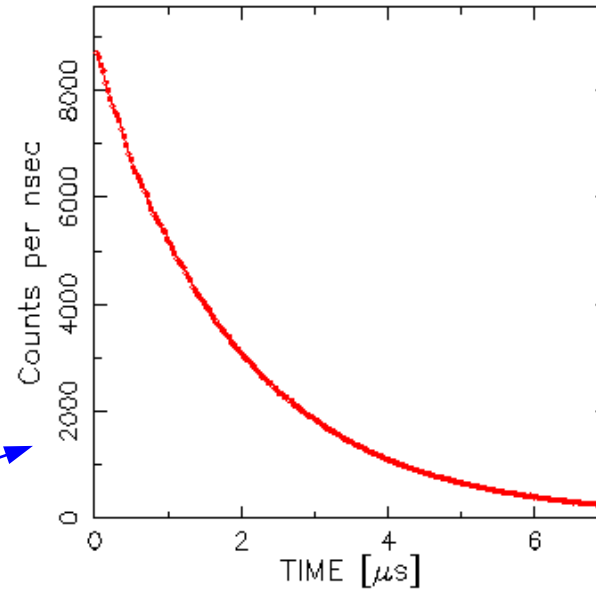
μ^-SR



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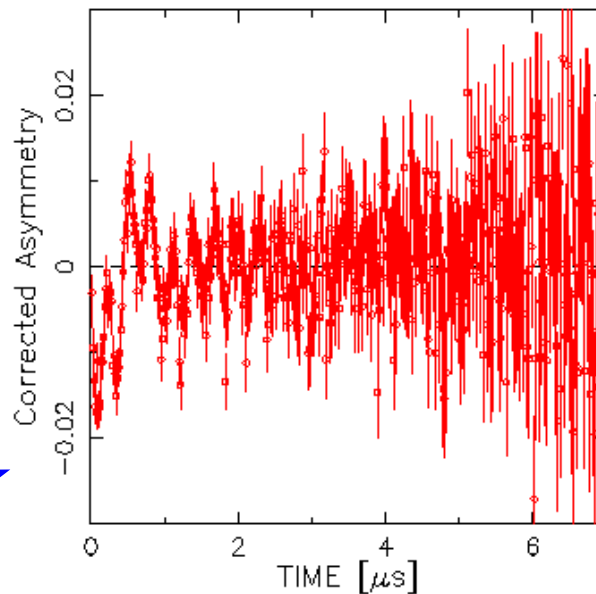
Multiple lifetimes (some very short!)



Asymmetry spectrum

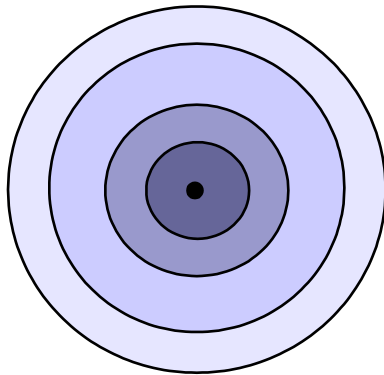
Large amplitudes

Small amplitudes



Atomic Capture & L•S Depolarization of μ^-

Large impact parameters are more probable
 \Rightarrow initial orbits tend to be **circular**.

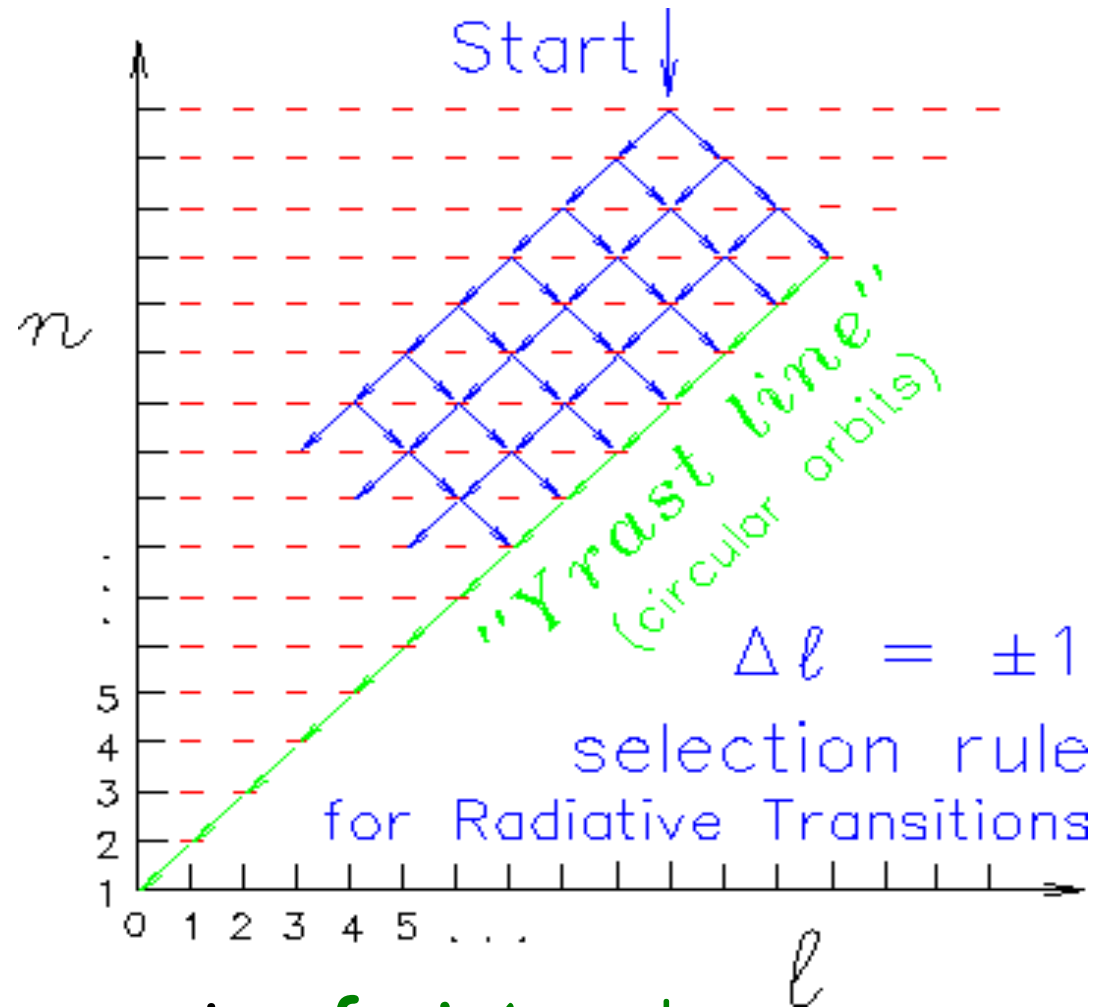


View along μ^-
 momentum

Primitive Atomic Physics:

$$r_n = \frac{a_0}{Z} \left(\frac{m_e}{m} \right) n^2$$

$$E_n = - \frac{13.6 \text{ eV}}{n^2} Z^2 \left(\frac{m}{m_e} \right)$$

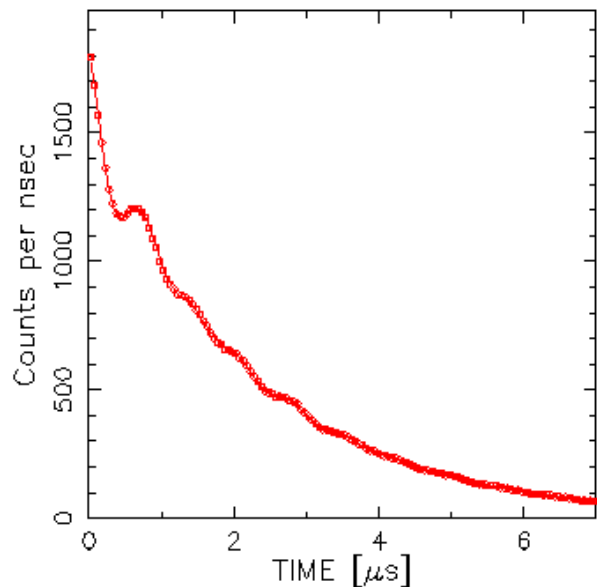


L•S couplings depolarize μ^- spin unless **fast Auger**!

μ^+SR

vs.

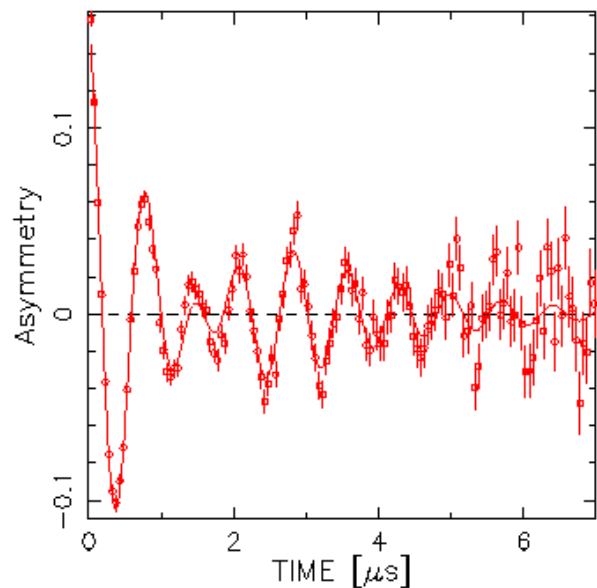
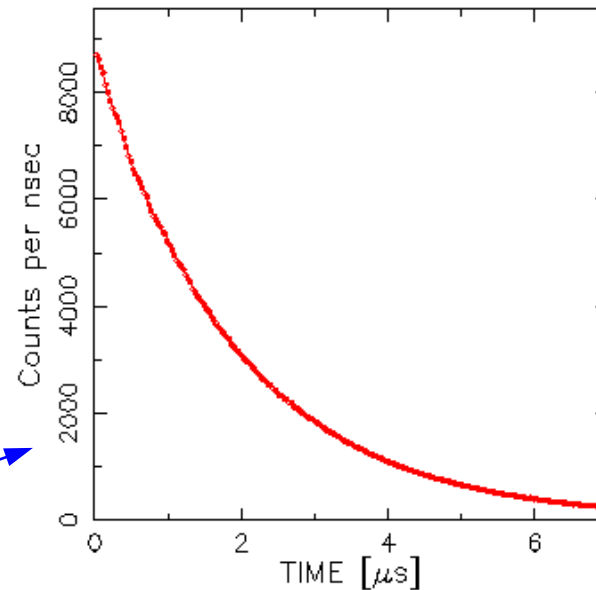
μ^-SR



Typical time spectrum (histogram)

Single lifetime $\tau_\mu = 2.197 \mu s$

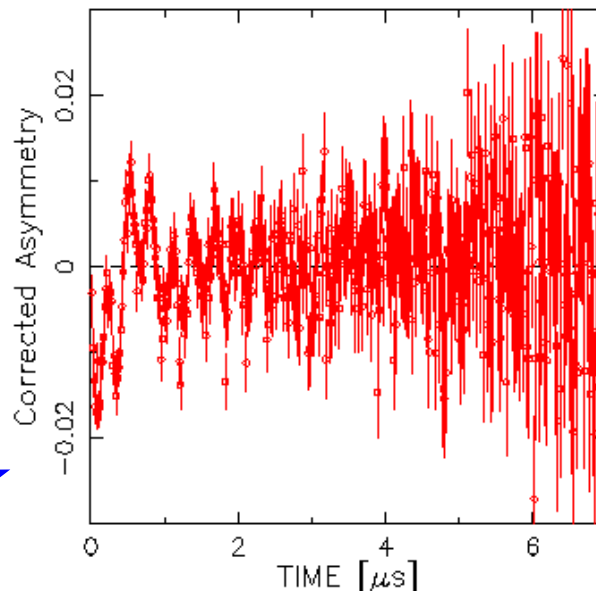
Multiple lifetimes (some very short!)



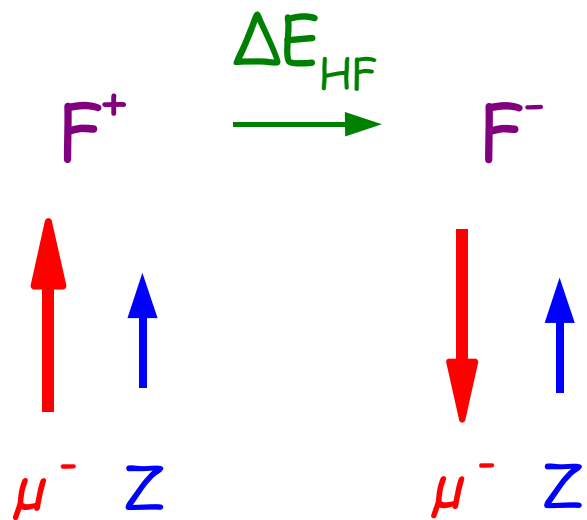
Asymmetry spectrum

Large amplitudes

Small amplitudes



Characteristic
precession
frequencies
of F^\pm
hyperfine states
in selected
low- Z
muonic atoms



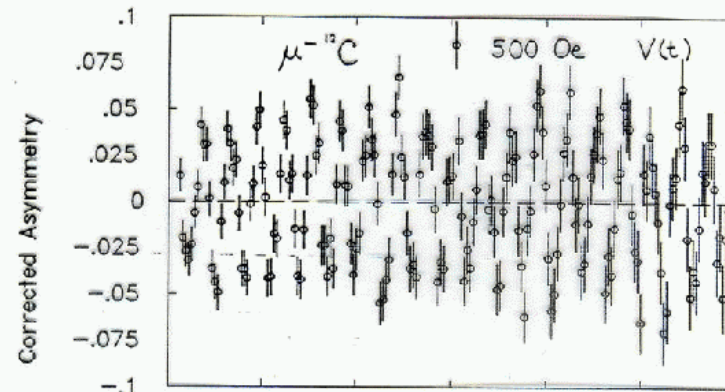
Isotope ${}^A E I_Z$	Nucl. Spin	Natural Abundance	Moment μ_N/μ_μ	Frequency Ratios	
				F^+/μ^-	F^-/μ^-
${}^1\text{H}_1$	1/2	≈ 1	-0.314109	0.342946	0
${}^2\text{H}_1$	1	≈ 0	-0.096436	0.301188	-0.397624
${}^6\text{Li}_3$	1	0.07	-0.092454	0.302515	-0.394969
${}^7\text{Li}_3$	3/2	0.93	-0.366253	0.158437	-0.402606
${}^9\text{Be}_4$	3/2	≈ 1	0.132447	0.283112	-0.194814
${}^{10}\text{B}_5$	3	0.19	-0.202528	0.113925	-0.181434
${}^{11}\text{B}_5$	3/2	0.81	-0.302380	0.174405	-0.375992
${}^{13}\text{C}_6$	1/2	0.01	-0.079000	0.460500	0
${}^{14}\text{N}_7$	1	≈ 1	-0.045394	0.318202	-0.363596
${}^{19}\text{F}_9$	1/2	≈ 1	-0.295666	0.352167	0
${}^{23}\text{Na}_{11}$	3/2	≈ 1	-0.249406	0.187648	-0.353919
${}^{25}\text{Mg}_{12}$	5/2	0.10	0.096197	0.182700	-0.144221
${}^{27}\text{Al}_{13}$	5/2	≈ 1	-0.409555	0.098408	-0.262229

TF- μ^- Spin Rotation in Muonic Atoms (μ^-Z) with NUCLEAR SPIN :

JHB 1982

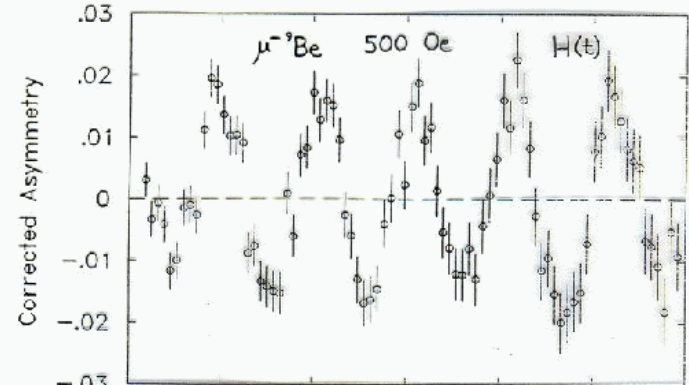
$$F^+ = I + \frac{1}{2}$$

$$F^- = I - \frac{1}{2}$$



$$I = 0$$

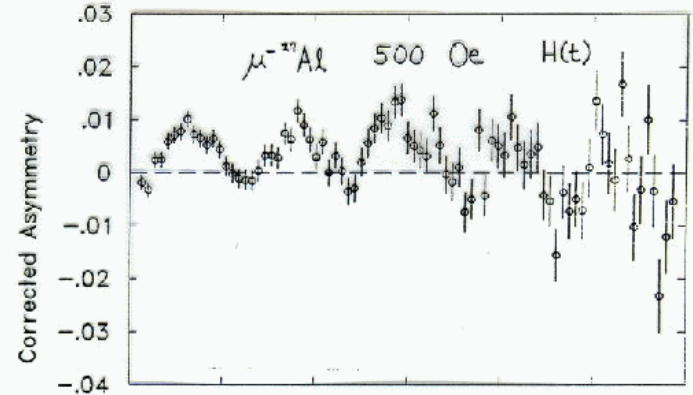
$$\nu = \nu_\mu$$



$$I = \frac{3}{2}$$

$$\nu_+ = 0.283\nu_\mu$$

$$(\nu_- = -0.195\nu_\mu)$$



$$I = \frac{5}{2}$$

$$(\nu_+ = 0.098\nu_\mu)$$

$$\nu_- = -0.262\nu_\mu$$

TIME (Microsec)

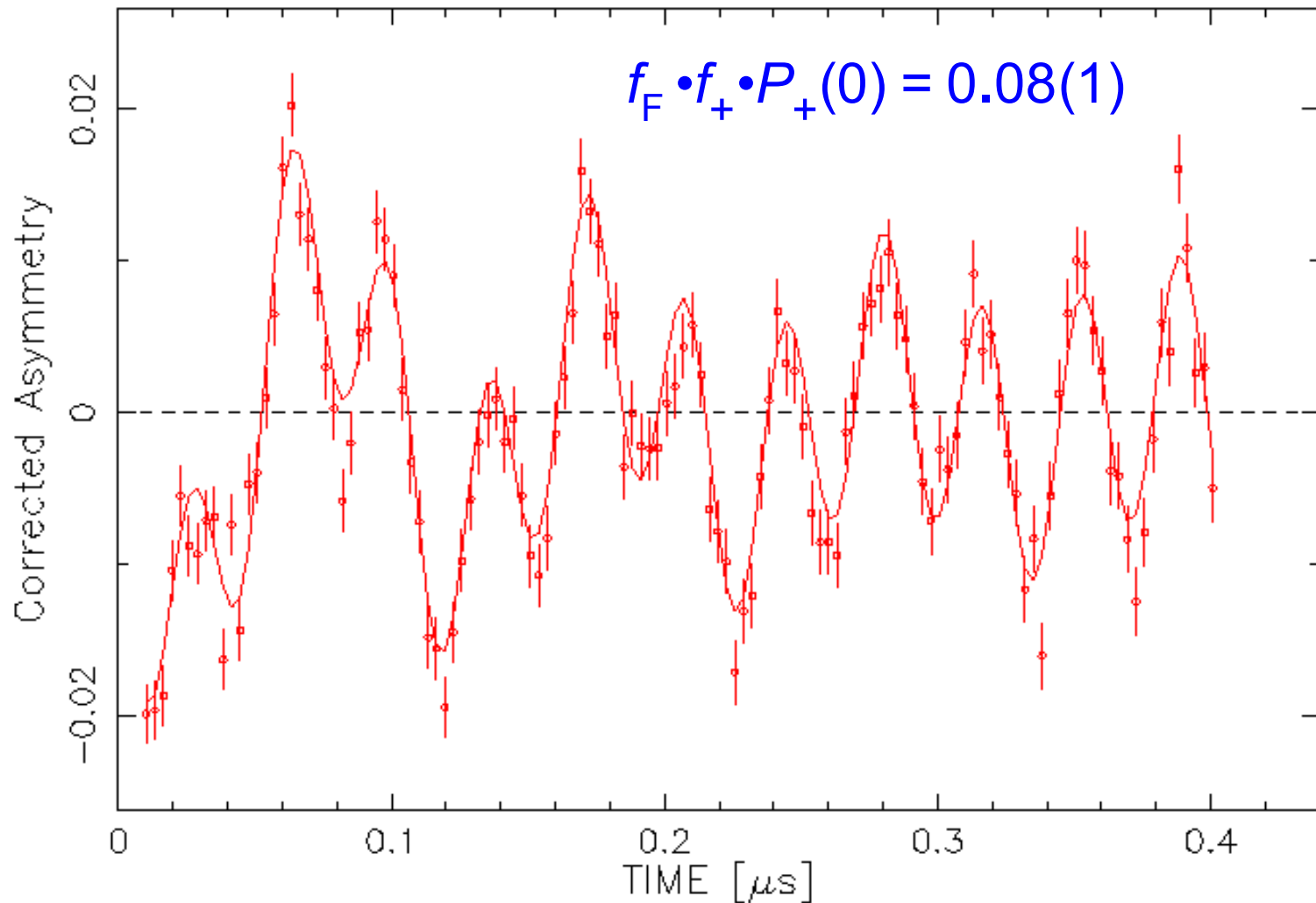
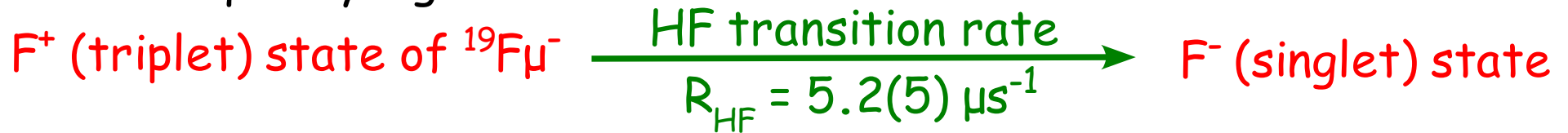
HFS OF SELECTED "BARE" MUONIC ATOMS:

$\mu^-(Z, A)$ ground state $\left\{ \begin{array}{l} F^+ = I + 1/2 \\ \Delta E_{HF} \\ F^- = I - 1/2 \end{array} \right.$

ELEMENT $\begin{smallmatrix} A \\ Z \end{smallmatrix}$	ΔE_{HF} (eV)	effective field B_{HF} (G)	Lowest e^- SHELL ejected [B.E. (eV)]	$F^+ \rightarrow F^-$ RATE R (μs^{-1})		REF
				THEOR	EXPT	
${}^1\text{H}_1$	0.1817	3.24×10^9	NONE	1.3×10^4	(ρ/ρ_0)	Ponomarev '78 smilga & Filchenko '83
${}^3\text{He}_2$	1.373	2.45×10^{10}	NONE	nil		
${}^{11}\text{B}_5$	18	3.2×10^{11}	L_1 [9.3]	0.25	0.33(5)	Winston '63 Favart et al '70
${}^{13}\text{C}_6$	11	2.0×10^{11}	L_2 [8.3]		0.016(12)	BOOM '83
${}^{14}\text{N}_7$	7.5	1.3×10^{11}	NONE	nil	0.092(33)	"
${}^{19}\text{F}_9$	126	2.2×10^{12}	L_1 [30]	5.8	6.1(7) [neutrons]	Winston '63
${}^{27}\text{Al}_{13}$	263	4.7×10^{12}	L_1 [89]	41	41(9)	" & Brewer '83
${}^{51}\text{V}_{23}$	1210	2.1×10^{13}	L_1 [565]	700		Winston '63
${}^{93}\text{Nb}_{41}$	~ 5000	$\sim 10^{14}$				
${}^{209}\text{Bi}_{83}$	4660	8.3×10^{13}	MEASURED VIA SPLITTING OF X-RAY ENERGY			

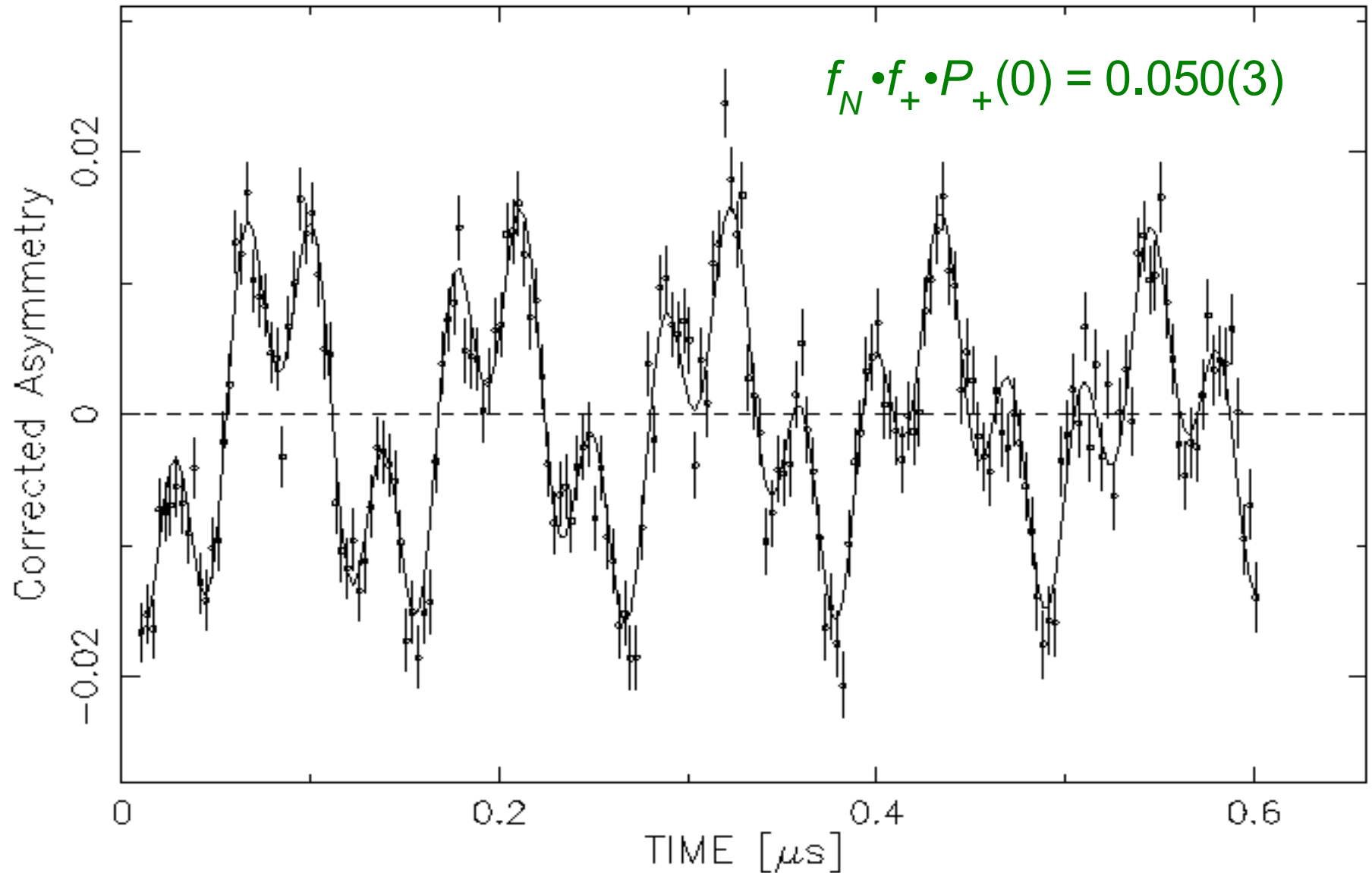
μ^-SR in Teflon $[(CF_2)_n]$: High frequency signal: μ^-C

Low frequency signal:



μ^-SR in Melamine ($C_3H_6N_6$):

High frequency signal: μ^-C Low frequency signal: F^+ state of $^{14}N\mu^-$



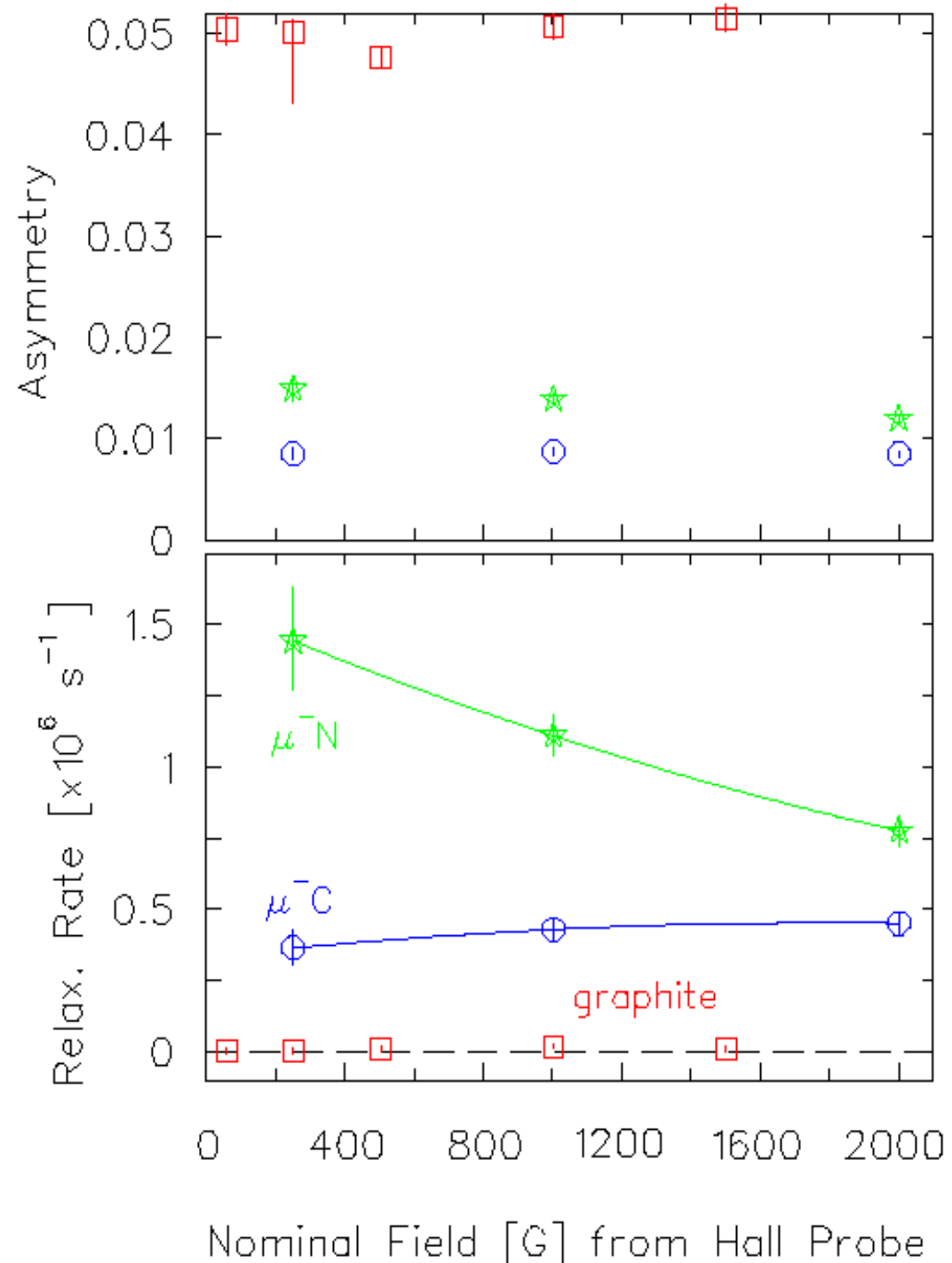
μ^-SR in Melamine ($C_3H_6N_6$)

$f_N \cdot f_+ \cdot P_+(0)$ decreases with B

Λ_N decreases with B

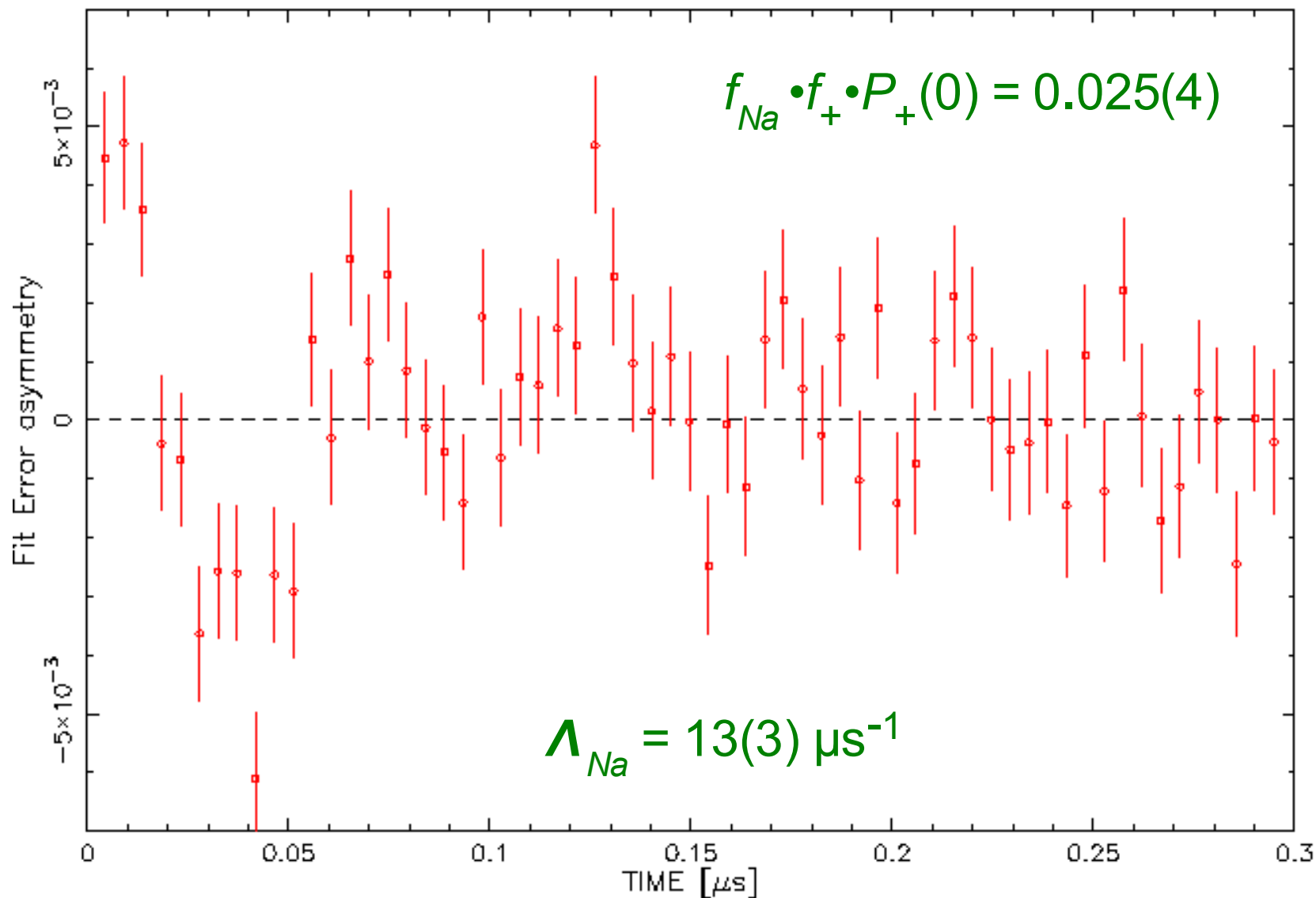
and is much too large
to be caused by either
 R_{HF} or neighbouring
nuclear dipoles.

Λ_C is also
anomalously fast.



First observation of μ^-SR in Sodium Metal

15368: 65 MeV/c μ^- in Sodium Metal Varian=-7086 G re-realigned [1 vs 2] ASY



Finis

Linux
and
OpenOffice
RULE!

"Themes" in $\mu^\pm SR$

μ^+ only (?)

Muonium as light Hydrogen

($\text{Mu} = \mu^+ e^-$)

($\text{H} = p^+ e^-$)

- **Mu** vs. **H** atom **Chemistry**:
 - gases, liquids & solids
 - Best test of reaction rate theories.
 - Study "unobservable" **H** atom rxns.
 - Discover new **radical** species.
- **Mu** vs. **H** in **Semiconductors**:
 - Until recently, $\mu^+ SR \rightarrow$ **only** data on metastable **H** states in semiconductors!
- **Quantum Diffusion**: μ^+ in metals (compare H^+); **Mu** in nonmetals (compare **H**).
- **Ultra-Heavy Hydrogen**: neutral muonic helium ($\alpha^{++} \mu^- e^-$) has $m \approx 4.11 m_H$

μ^+ or μ^-

The Muon as a Probe

- **Probing Magnetism**: unequalled sensitivity
 - Local fields: electronic structure; ordering
 - Dynamics: electronic, nuclear spins
- **Probing Superconductivity**: (esp. $\text{HT}_c \text{SC}$)
 - Coexistence of SC & Magnetism
 - Magnetic Penetration Depth λ
 - Coherence Length ξ

μ^-SR :

It is easy to get the impression that **only positive** muons are employed in μSR .

Although most μSR is μ^+SR , it is often desirable to use **negative** muons in the same way, albeit with more **difficulty**.

DRAWBACKS of μ^-SR



PROPOSED MITIGATIONS

- **L•S** Depolarization in the atomic cascade
- Nuclear Muon Capture: short lifetimes, few decay e^-
- Giant Hyperfine Interaction with nonzero-spin nuclei



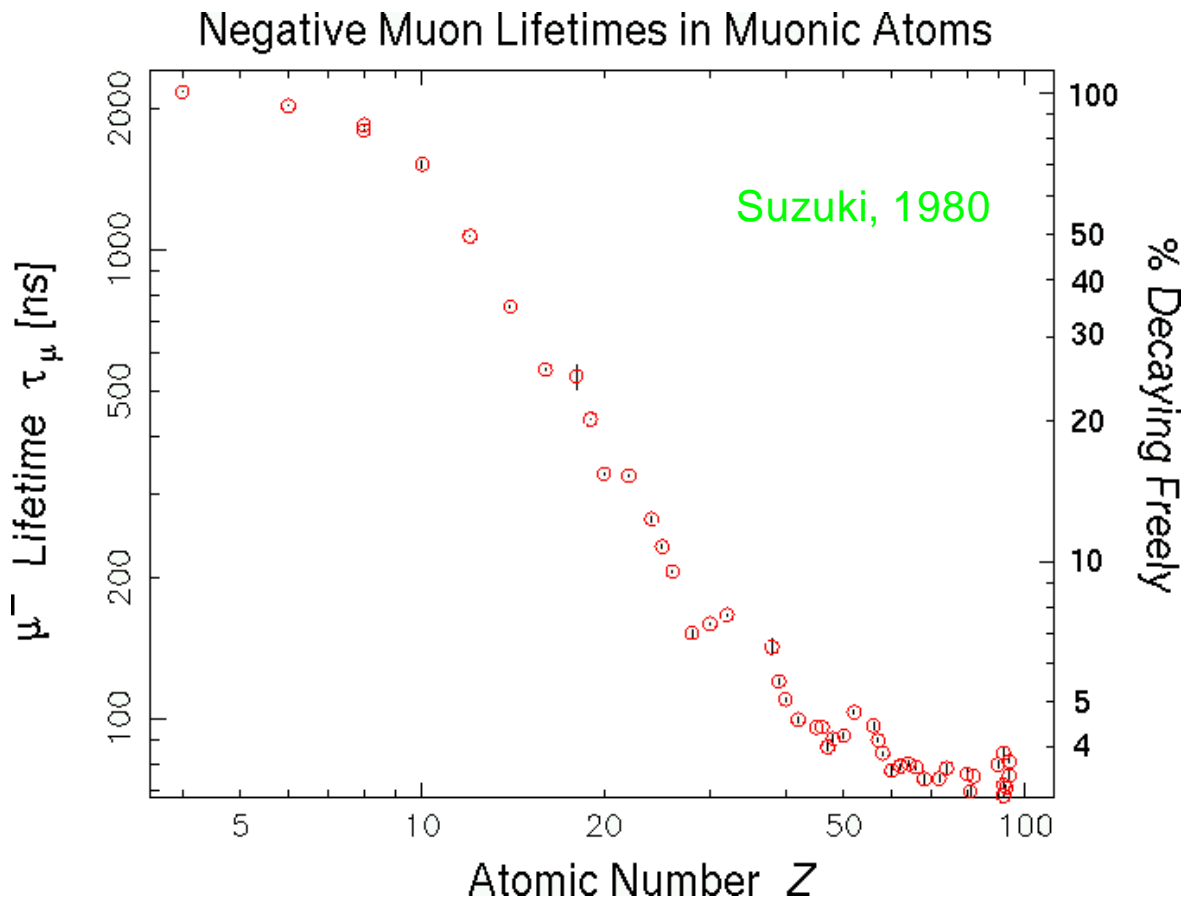
"Tag" events with specific muonic X-rays



Look for neutron asymmetries in heavier elements



Observe characteristic F^\pm precession signals



Nuclear μ^- Capture

PROBLEM

$\mu^- p \rightarrow n \nu_\mu$ in a nucleus:
rate comparable to that
of

$\mu^- \rightarrow e^- \nu_\mu \nu_e$ for $Z \geq 10$.

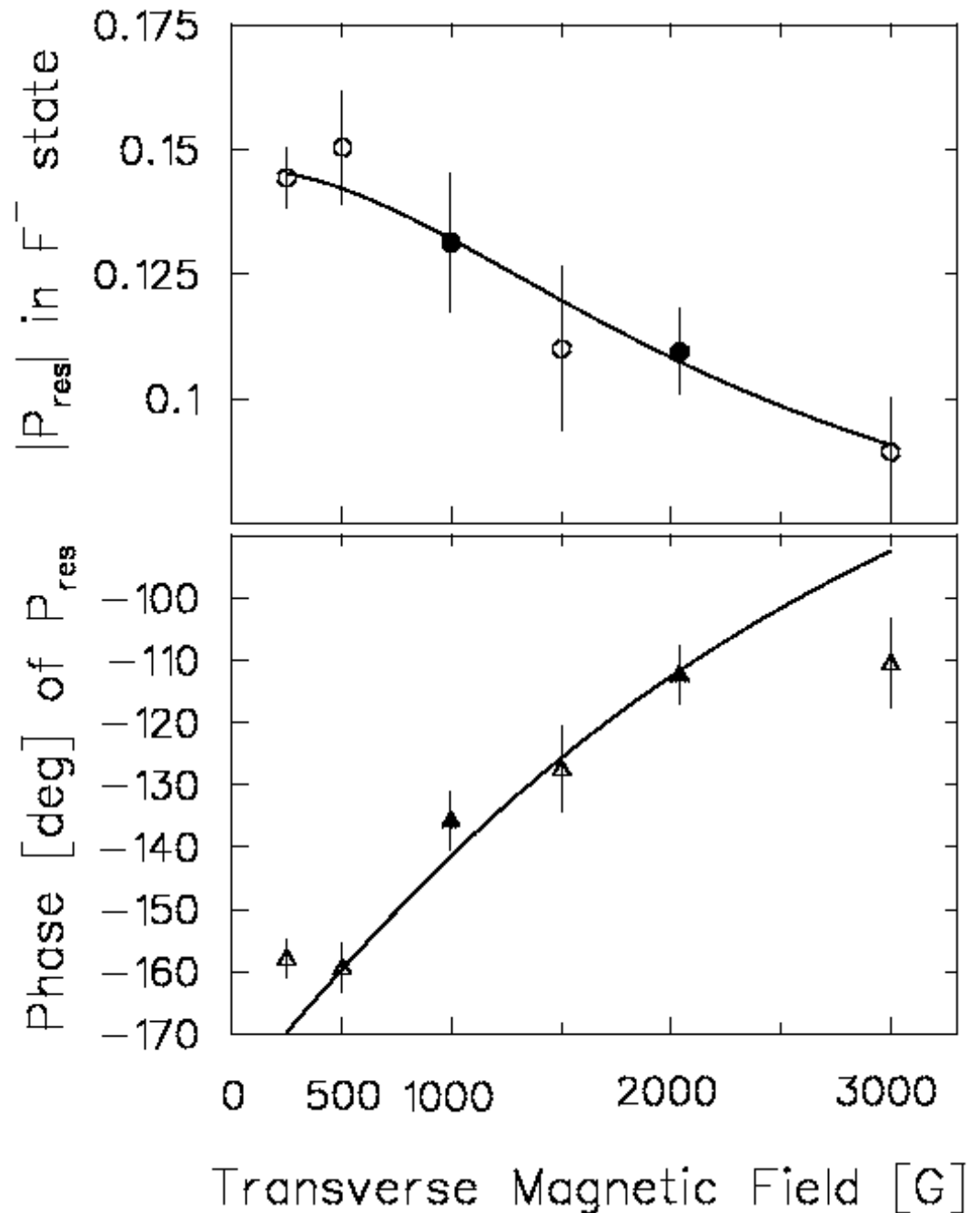
Possible Help: Many times a **fast neutron** is emitted from nuclear μ^- capture. Very few measurements have been made of the correlation of that neutron with the muon's spin direction. If cases are found where this **neutron asymmetry** is sizeable, we may be able to do **neutron-triggered μ^-SR** , for which the event rate can be **higher** than in **μ^+SR** .

μ^-SR in ^{27}Al :

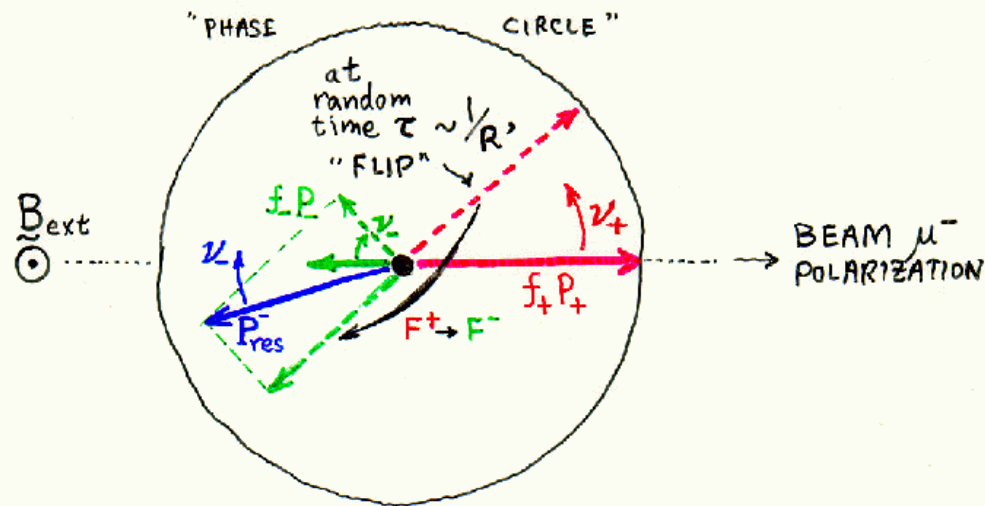
Residual F^- polarization
after initial precession
in F^+ HF state followed
by spin-flip transition
to F^- state

R_{HF} due to Auger
of core electrons:
measured value
is consistent with
the calculation of
Winston (1963):

$$R_{HF} \approx 41 \mu s^{-1}.$$



" P_{res}^- (B) METHOD" FOR MEASURING $f_{\pm} P_{\pm}$ & R
 for LARGE R :



- MECHANISM RESULTS IN "EASILY" VISIBLE F^- PRECESSION FOR "ALL" $Z \gtrsim 20$ (i.e., where R is too fast to allow direct observation of F^+ state). (even in ^{93}Nb ! [?])
- In some cases (e.g., ^{23}Na or ^{27}Al), studying P_{res}^- (B) [APPARENT INITIAL AMPLITUDE & PHASE of F^- SIGNAL] as a function of field

allows determination of $f_+ P_+$ and $f_- P_-$.

E.g., in ^{27}Al , $f_+ P_+ = 0.21(9) P_0$ vs 0.333 THEOR.
 $f_- P_- = +0.045(20) P_0$ vs NEGATIVE predicted value!

NEED MORE DATA to
 CHECK BUKHVOSTOV!

Relativistic Shift of μ^- Frequency

